

Calculus, Zombies, Community, and QUBES:

**Education at the
interface of
mathematics and biology**

Carrie Diaz Eaton

Unity College

Math and biology education

Mathematical biology

Quantitative biology

Quantitative skills for biologists

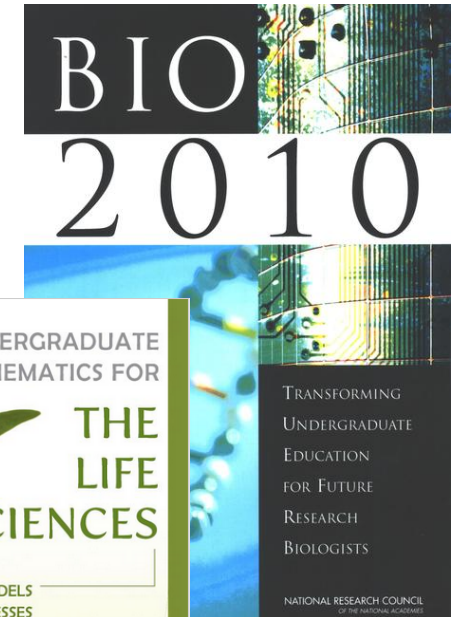
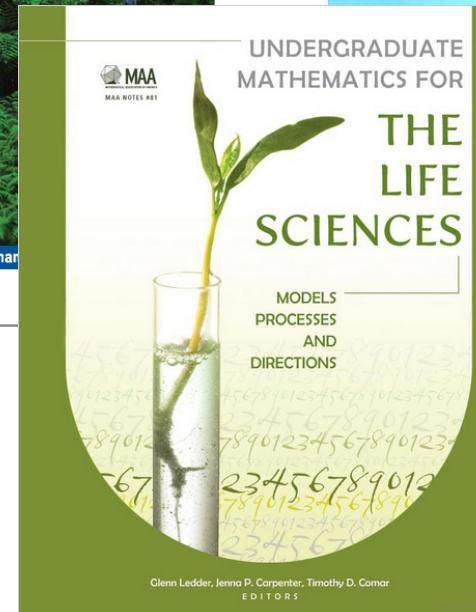
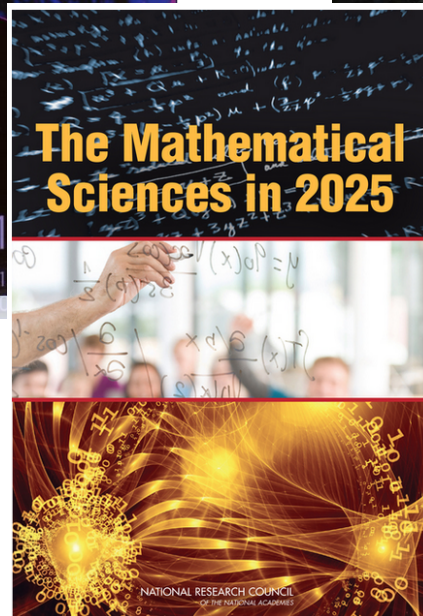
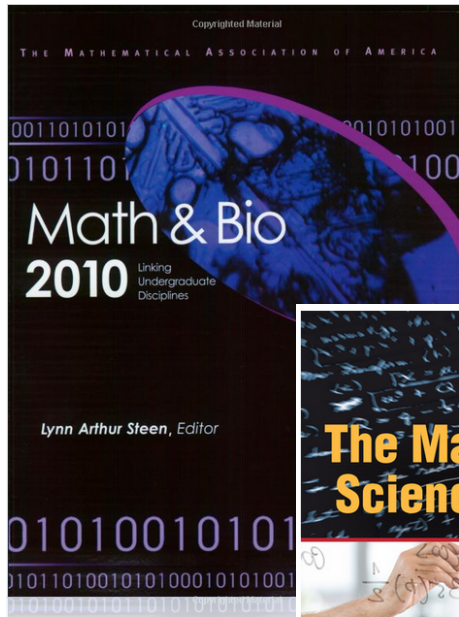
Quantitative literacy for biologists

Biology

Life science

Environmental and biological sciences

Math and biology education



Why is math good for biology?

Reports -

Bio 2010, Vision and Change, PCAST

- Helps advance theory in biology (*e.g.* Servedio, 2014)
- To interpret the output and understand the assumptions of computational tools (*e.g.* bioinformatics)
- Helps process large amounts of data (*e.g.* genome sequencing, ecological indicators).

Why should math consider serving biology?

- To meet the needs of all students - Life science students may underperform in traditional math courses
- PCAST report - if we don't do it right, let the biologists do it
- Adjusting requirements by biology programs may reduce math requirements
- To uncover latent talent
 - Did you know I was a life science student first?

Working together might look like...

- Aligning content of prerequisite or corequisite courses to companion courses
- Changing biology program requirements
- Designing special life science-focused math and statistics courses
- Integrating biology-oriented examples or projects into math courses
- Emphasizing quantitative skills in biology courses
- Interdisciplinary student research opportunities

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Example - redesigning Calculus

- Environmental college in Unity, Maine
 - ~600 undergraduates
 - Interdisciplinary Centers (Carrie Diaz Eaton in Center for Biodiversity)
 - No math department, no math major
 - Hands-on learning and environmental and ecological emphasis
- Academic Master Planning (AMP) in prep for accreditation review by NEASC - push to 40-40-40

Example - Redesigning Calculus

- Calculus required by Wildlife Biology, Earth and Environmental Science
- Option for Biology*, Marine Biology*, and Sustainable Energy Management
- Population management and climate change drive Calculus content, not MCATs
- History of co-teaching/collaborative course design

*Required prior to AMP (& Wildlife)

Course Design (Unity)

Surveys and follow-up interviews

(UC IRB #2011-06)

1. It must be called Calculus (external requirement)
2. It must be rigorous (*je ne sais quoi*)
3. It must deepen the understanding of foundational principles in modeling feedback and interactions (in complex systems)

Course Design (Unity)

Book: Mathematics for Life Science, Bodine, Gross, and Lenhart

Calculus I (3-credit, no lab)

- **Sequences**
- **Linear discrete-time models and equilibria**
- Limits
- Continuity
- Derivatives
- Optimization
- **Modeling with ordinary differential equations**
- **Exponential models and equilibria**
- **Partial derivatives**

Low-stakes reflectionary writing

Group professional recommendation

Group lab reports

Excel

Calculus II (3-credit, no lab)

- Integration
- Series
- Antiderivatives
- **Continuous probability distributions**
- **Exact solutions to 1-D separable (ODEs)**
- **Bifurcations and tipping points**
- **Numerical solutions and qualitative analysis of 1-D and 2-D autonomous ODEs**

Readings and discussion on complex systems and computing

Individual lab-reports with peer review (Eaton and Wade, 2014)

MATLAB

Eaton and Callender (submitted to CBE)

Calculus I Learning Outcomes (Unity)

Content

1. Interpret **sequences, limits, and continuity** algebraically, numerically, visually, and verbally.
2. Interpret **derivatives** algebraically, numerically, visually, and verbally.
3. **Model** simple scenarios of **change** through either difference equations or differential equations.
4. **Apply** principles of **derivatives** to optimization and relative change.

Disposition

5. **Recognize** limits and derivatives in the **practical and professional** world, particularly in environmental and life science.
6. **Investigate** problems using a **computer** algebra system or spreadsheet system.
7. Work in **groups** to investigate problems and **communicate** solutions on an introductory level.
8. Practice time management and **discipline** in self-paced study.

BEER Intervention

Faculty all over are working on the same problem, at different places, not knowing.

BEER changed all that.

BEER Intervention

We were both working on the same problem,
two different places, not knowing.

BEER changed all that.



BEER Intervention

We were both working on the same problem,
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No, not that kind of beer...

BEER Intervention

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No, not that kind of beer...
the International Symposium on
Biomathematics and **E**cology
Education and **R**esearch

Assessment and Results

Content Outcomes Assessment

> MATH PERFORMANCE

Dispositional Outcomes Assessment

> ATTITUDES AND PERCEPTIONS

Lots of case studies, anecdotal.

We share lots of experiences and ideas, but how are we doing at assessment of those implementations?

Assessing Math Performance - At risk pop now as good as or better

Unity College - assessment through CCI
(Epstein, 2013)

- High pass rates, low W rates
- Average of approximately 17% learning gain for 3-credits (4 semesters, 5 sections)
- Perhaps equivalent to about 25% for 4-credit (CCI Traditional [-?, 21]% and IE [21,44]%)

University of Portland - assessment through common quiz compared to traditional calculus

- Biocalculus students scored better (t-test significant) on final

Attitude Results - UP and UC

Positive change in attitudes

Students showed a significant change ($p\text{-value} < 0.05$) or near (< 0.10) Wilcoxon signed-rank, non-parametric:

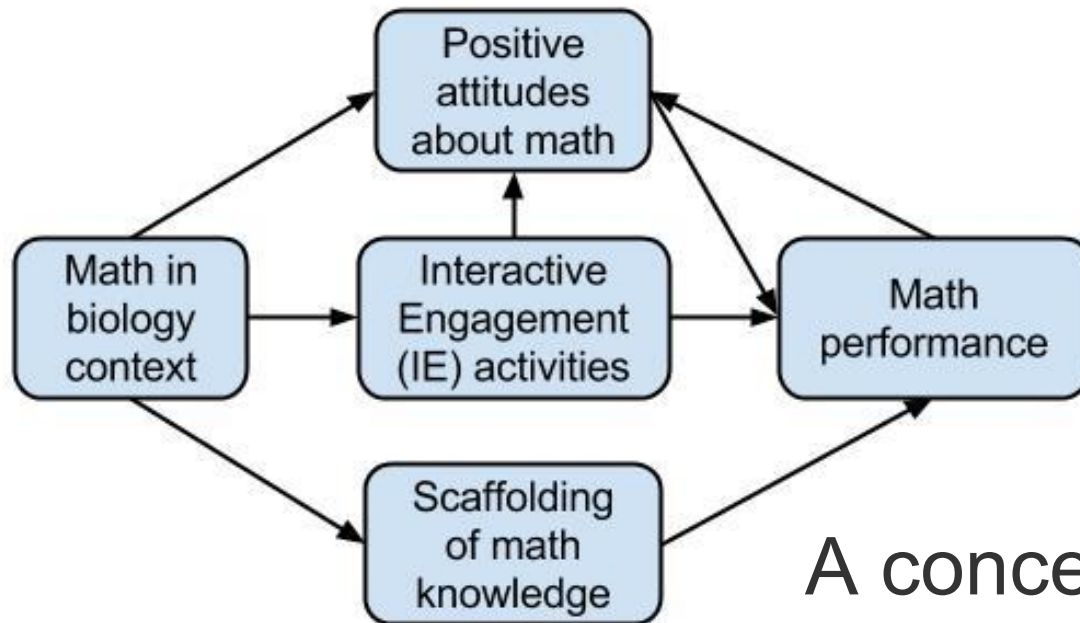
- *Students agree more that their **attitude** towards math **affects their ability** to do math.
- Students **disagree** more **that ordinary students cannot expect to understand mathematics**, they expect simply to memorize it and apply what they have learned mechanically without an understanding.
- Students agree more that math is **creative** and they can **discover** things on their own.
- Students agree more that try to learn mathematics because it **helps develop their mind** and helps them think more clearly in general.

Attitude Results - Unity specific

For UC, the questions that yielded a significant difference ($p\text{-value} < 0.05$), but not for UP were

- Students agree more that using the web or **computer can help them learn mathematics**. (*Excel for exploration, 6*)
- Students **disagree** more that **math is a solitary** activity (*Work in teams, 7*).
- Students agree more that the **skills** they learn in this class will **help them in other classes**. (*Math in context, working directly with stakeholders, 5*)

Why teach biology driven math?



A conceptual model

- Bigger picture through collaboration
- Adds to picture bigger picture of what works and what doesn't
- BEER intervention

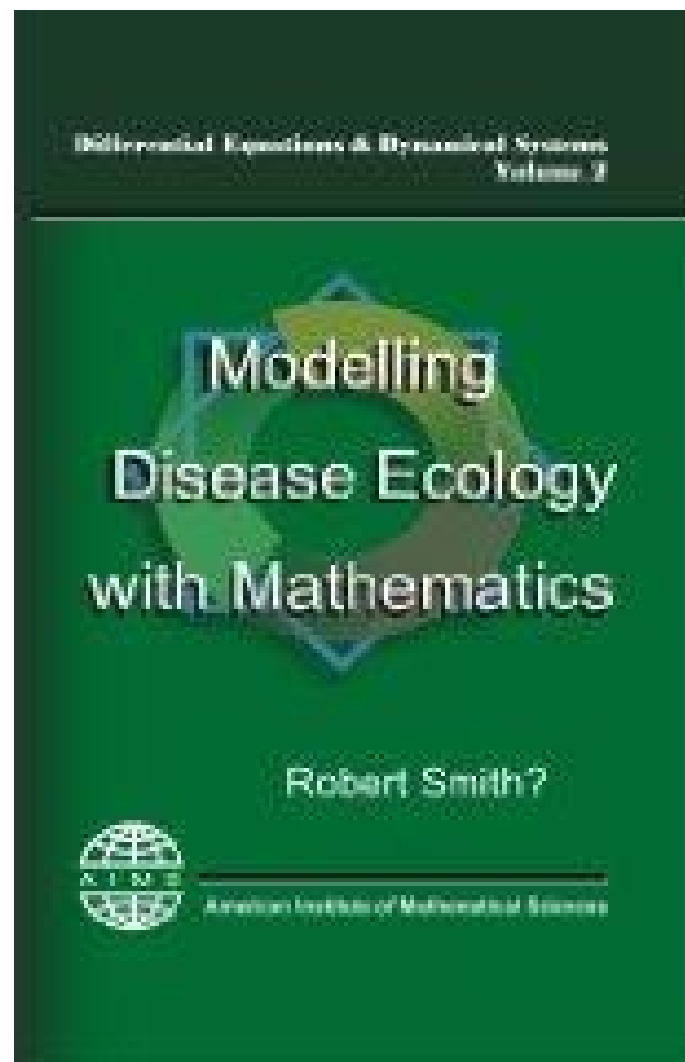
Example - Undergraduate Research

Students can go from
Calculus II to and ODE
modeling course

SIR modeling

Other ODEs like predator-
prey interactions

Zombies and Ticks



Zombies are fictional undead creatures regularly encountered in horror and fantasy themed works. They are typically depicted as mindless, reanimated corpses with a hunger for human flesh, and particularly for human brains in some depictions.

- wikipedia



- Night of the Living Dead

$$TSP = 5250$$

$$RSP = 14525$$

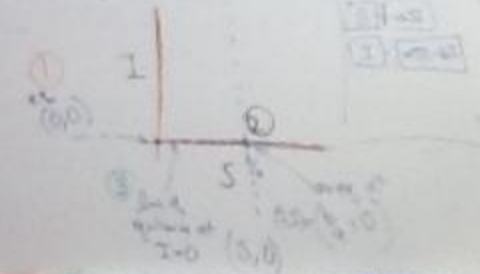
$$\frac{\partial f}{\partial S} = 1.25$$

$$\frac{\partial f}{\partial I} = 0.25$$

$$X = 15750$$

$$P = 950000$$

$$b = 815750$$



$$S' = aS - bSI$$

$$I' = bSI - aI$$

$$J = \begin{pmatrix} \frac{\partial f}{\partial S} & \frac{\partial f}{\partial I} \\ \frac{\partial g}{\partial S} & \frac{\partial g}{\partial I} \end{pmatrix}$$

$$\frac{d}{dt} \begin{pmatrix} S \\ I \end{pmatrix} = \begin{pmatrix} -aS \\ aSI - bI \end{pmatrix} f(S, I)$$

$$J = \begin{pmatrix} \frac{\partial f}{\partial S} & \frac{\partial f}{\partial I} \\ \frac{\partial g}{\partial S} & \frac{\partial g}{\partial I} \end{pmatrix} \quad \frac{\partial f}{\partial S} = -aS = -aI \quad \frac{\partial f}{\partial I} = bS = -aI \quad \frac{\partial g}{\partial S} = aSI - bI = aI \quad \frac{\partial g}{\partial I} = aSI - bI = aI$$

$$J = \begin{pmatrix} -aI & -aS \\ aI & aS - b \end{pmatrix}$$

BRIDGE WATER FOR NAME'S DATE

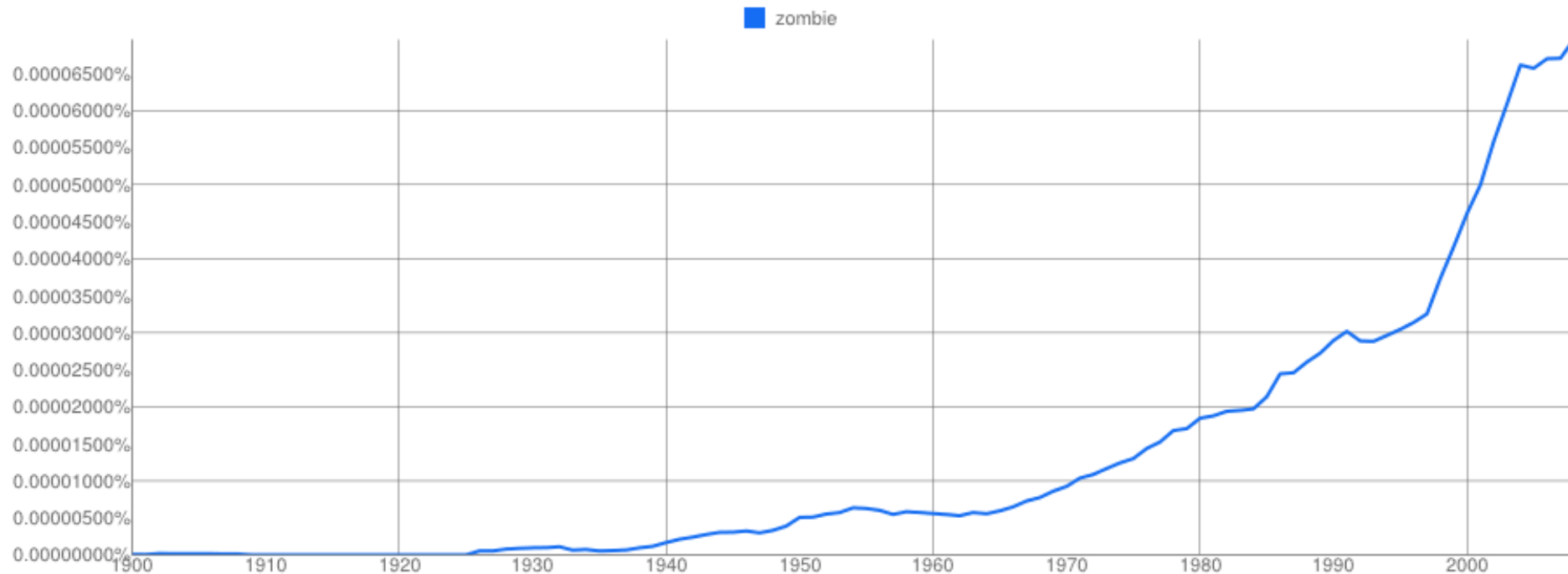


Modeling Disease Ecology with Mathematics

Graph these **case-sensitive** comma-separated phrases:

between and from the corpus with smoothing of .

[Search lots of books](#)



Search in Google Books:

1900 - 1966	1967 - 2002	2003 - 2004	2005 - 2006	2007 - 2008	zombie (English)
-----------------------------	-----------------------------	-----------------------------	-----------------------------	-----------------------------	----------------------------------

Increasing in popularity



PREPAREDNESS 101:

ZOMBIE PANDEMIC



U.S. Department of
Health and Human Services
Centers for Disease
Control and Prevention

Zombie Apocalypse: Bangor, Maine Prepares For Hordes Of Undead Minions

The Huffington Post | By Andy Campbell



Posted: 06/24/2012 9:36 am Updated: 06/24/2012 10:14 am



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1,583

86

23

155

406

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comment

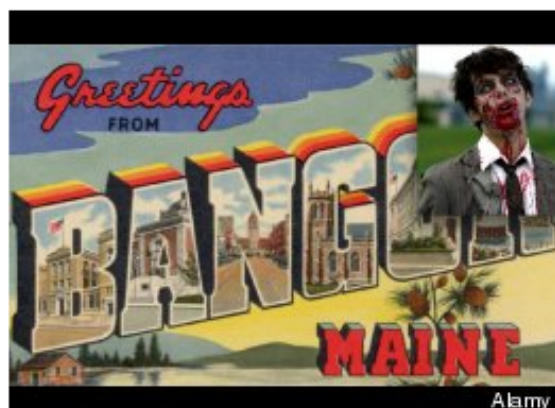
GET WEIRD NEWS ALERTS:

Enter email

SIGN UP

REACT: [Amazing](#) [Inspiring](#) [Funny](#) [Scary](#) [Hot](#) [Crazy](#) [Important](#) [Weird](#)

FOLLOW: [Zombies](#), [Bangor](#), [Bangor Zombies](#), [Maine](#), [Pandemic Preparedness](#), [Zombie Apocalypse](#), [Zombie Preparedness](#), [Zombies Take Over Maine](#), [Weird News](#)



Grab your **zombie bullets** and your running shoes, the undead have reached Maine!

Just days after the **federal government** **denied the existence** of zombies, the city of Bangor took the zombie apocalypse craze to a whole new level. Officials began **"preparing" for the undead** by running a daylong pandemic exercise Thursday that

res?um=1&hl=en&sa=N&rlz=1C1CHMO_enUS483...

Bangor Daily News reported

The Zombie War is Coming

About Humans vs. Zombies

WHAT IS HUMANSVSZOMBIES?

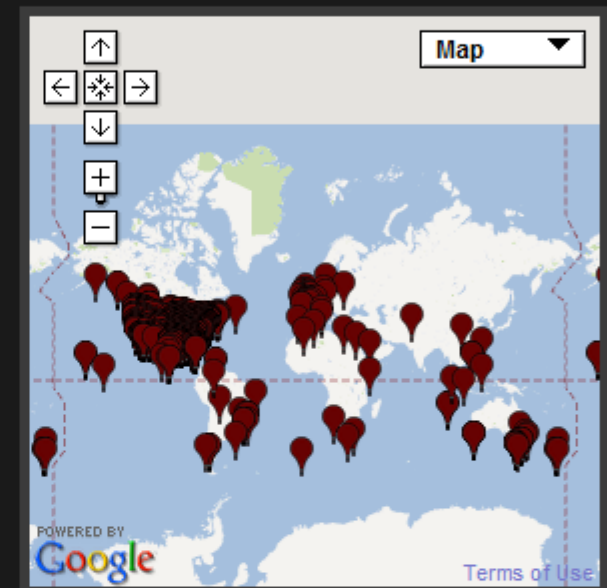
Humans vs. Zombies (HvZ) is a game of moderated tag played at schools, camps, neighborhoods, military bases, and conventions across the world. Human players must remain vigilant and defend themselves with socks and dart blasters to avoid being tagged by a growing zombie horde. [Read more](#), or [watch the documentary](#).



Since beginning at Goucher College in 2005, Humans vs. Zombies has developed an international fan base and received prominent press coverage from the [New York Times](#), the [Washington Post](#), [NPR](#), the [Associated Press](#), [FOX "News."](#) and Stephen Colbert, who named us the [number one threat to America](#). HvZ is played on six continents, with games in diverse locations such as [Australia](#), [Namibia](#), [Spain](#), and [Denmark](#).

Humans vs. Zombies is always free to play, and made available under a Creative Commons license.

Get Involved



[ADD YOUR SCHOOL TO THE MAP](#)

Find us on Facebook



Humans Vs. Zombies



Humans Vs. Zombies

Just 4 more days until the



HVZ

HUMANS VS ZOMBIES

"The antidote for the ailments of a generation."

- The International Herald Tribune



ABOUT HVZ

THE RULES

PR

Humans vs Zombies: Outbreak at Unity College

jacpac007



Subscribe

6 videos



8:56 / 9:53



HUMAN RULES



Staying On Campus: Humans must sleep on campus. If you need to leave campus for longer than 24 hours, contact the game moderators and remove yourself from the game.

I.D. Number: Humans must keep an index card with their unique identification number on them at all times.

Stunning a Zombie: Humans may stun a Zombie for 15 minutes by blasting them with a dart blaster or throwing a sock at them.

When Tagged By a Zombie: When tagged by a Zombie, a Human is required to distribute their ID card. One hour after being tagged, tie your bandanna around your head – you are now a member of the Zombie team! Go tag some Humans.

Wearing a Bandanna: Humans must wear a headband around an arm or leg to identify them as players of the game. (This headband will come in handy when you become a zombie!)

ZOMBIE RULES

Feeding: Zombies must feed every 48 hours. A zombie feeds by reporting their tag on the website.

Wearing A Headband: Zombies must wear a bandanna around their heads at all times. The Original Zombie does not need to wear a headband.



HvZ

Game of
tag to
spread
zombie
disease

Chapter 4

WHEN ZOMBIES ATTACK!: MATHEMATICAL MODELLING OF AN OUTBREAK OF ZOMBIE INFECTION

Philip Munz^{1*}, Ioan Hudea^{1†}, Joe Imad^{2‡}, Robert J. Smith^{2§}

¹School of Mathematics and Statistics, Carleton University,
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²Department of Mathematics, The University of Ottawa,
585 King Edward Ave, Ottawa ON K1N 6N5, Canada

²Department of Mathematics and Faculty of Medicine, The University of Ottawa,
585 King Edward Ave, Ottawa ON K1N 6N5, Canada

Abstract

Zombies are a popular figure in pop culture/entertainment and they are usually

UC HvZ game 2012, 2013

$$\frac{dH}{dt} = -k_1 HZ$$

$$\frac{dW}{dt} = -k_2 WZ$$

$$\frac{dZ}{dt} = k_1 HZ + k_2 WZ - bZ$$

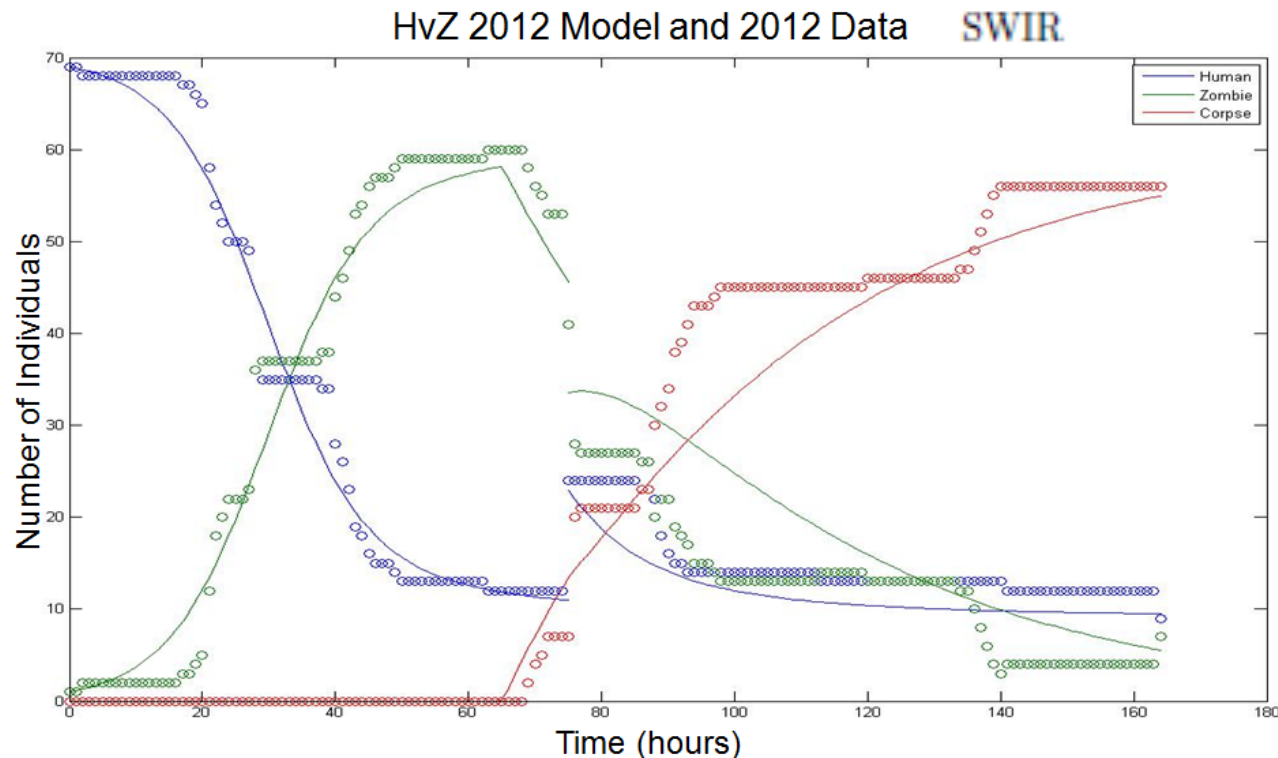
$$\frac{dC}{dt} = bZ$$

Parameter	Meaning
H	Humans
W	Warriors
Z	Zombies
C	Corpses
k_1	Rate constant H to Z
k_2	Rate constant W to Z
b	Rate constant Z to C

UC Game 2012

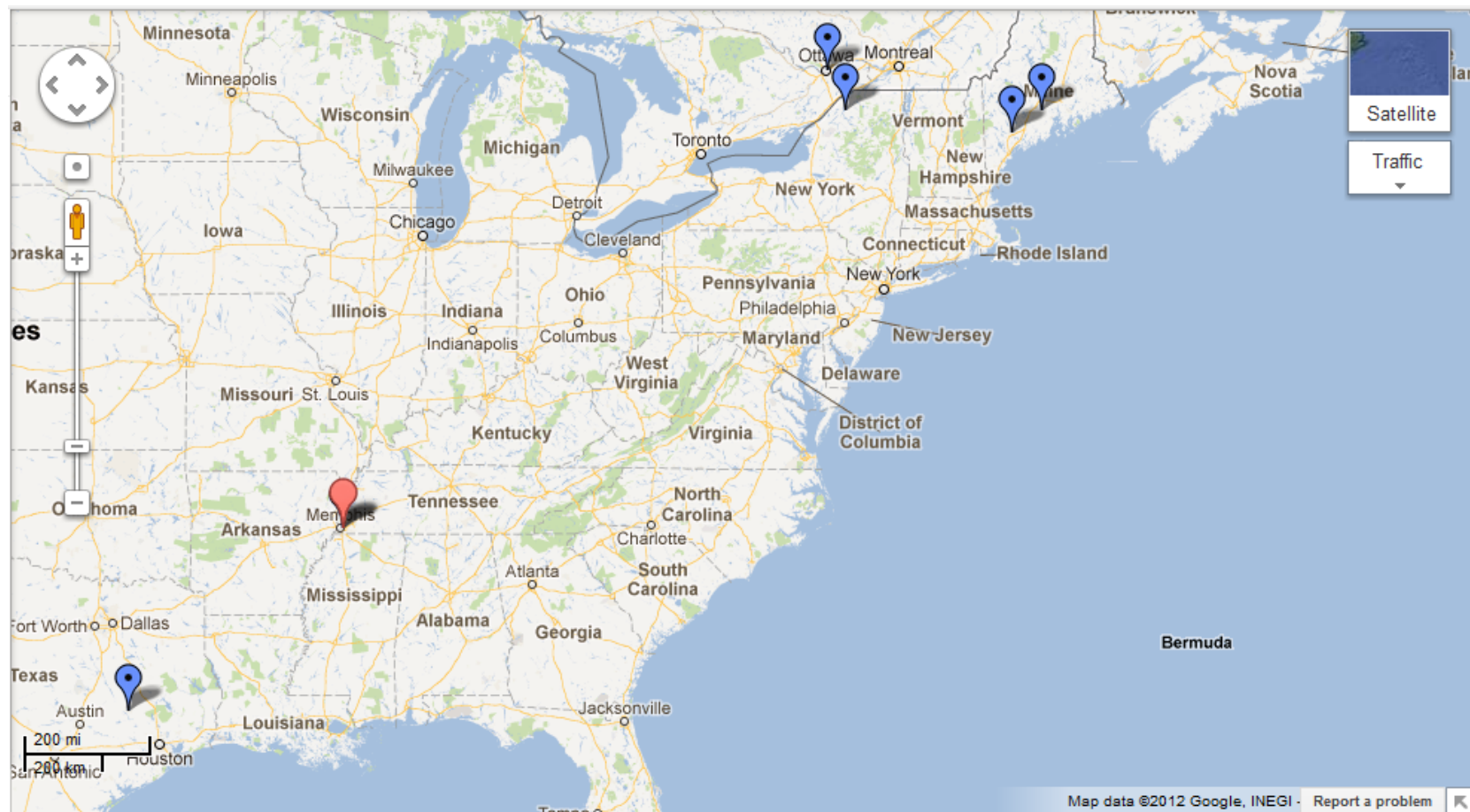
SWIR model

Phased Model Name	SSE	K	AIC
SIR	39208	4	923
Type II predator-prey	66772	6	1021
Type III predator-prey	73908	6	1038
Sinusoidal sleep cycles	53158	5	978
SIR	52606	2	961
SWIR	51388	3	963



Lemelin and Eaton (2015, under revision for Letters in Biomathematics)

Some of the Math Zombie research sites



We should be working together - meta-analysis!

QUBES: Quantitative Undergraduate Biology Education and Synthesis



math biology teachin

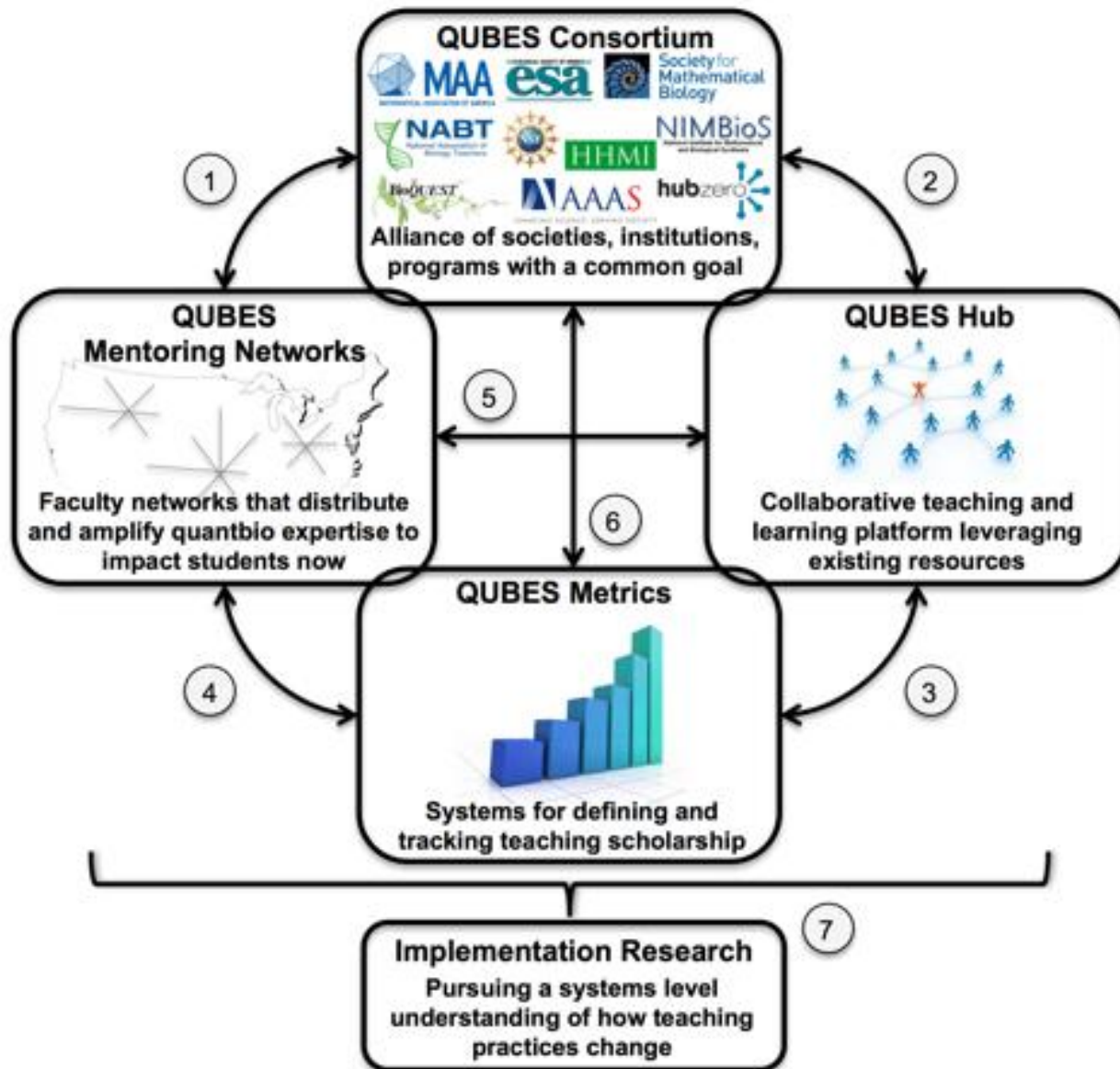


teaching math in biology

Press Enter to search.

The **synthesis** problem: Entities from mathematics and biology are working **independently** to create curriculum, content, and **educational experiences**, at the interface of these two fields, with the intended audience both **mathematics and biology** students.

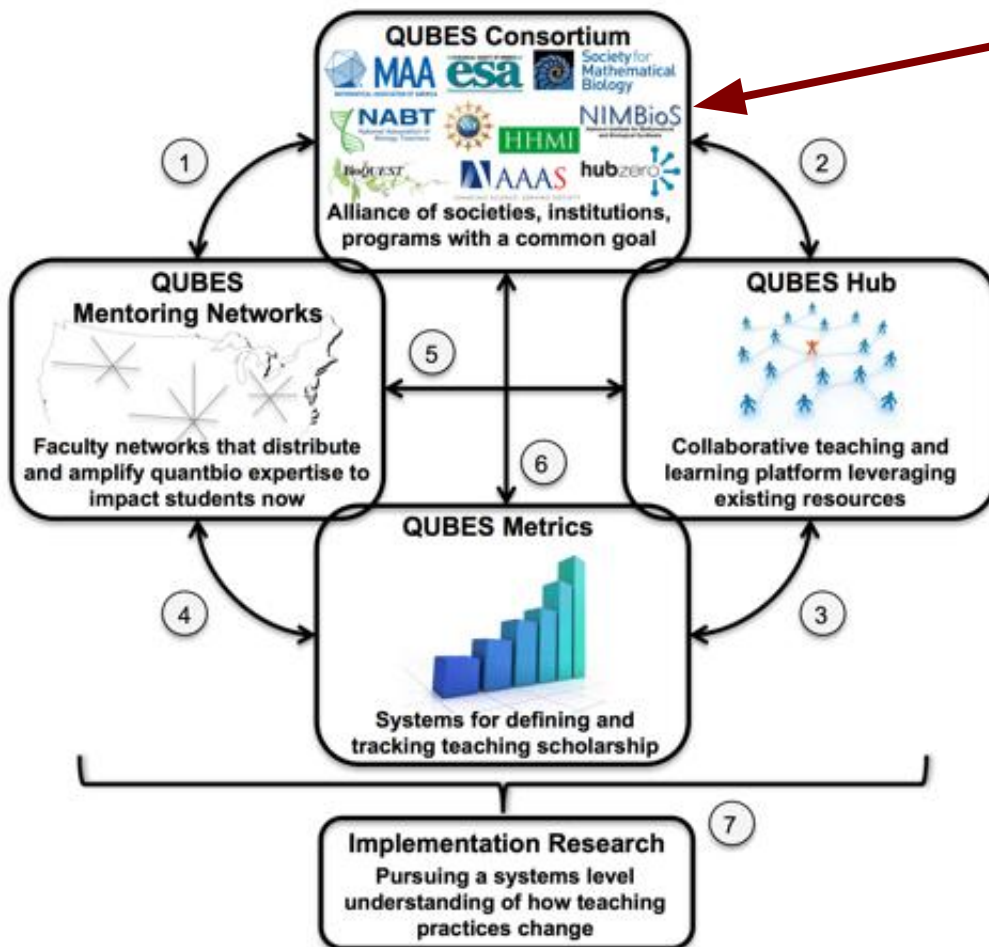
How do we bring it all together??



Scope of work
under the
\$2.9 million
NSF IUSE
Ideas Lab
grant.

- W&M,
- Unity College,
- Roanoke College,
- Radford,
- UPitt,
- UW, and
- BioQUEST

QUBES Consortium



- Communications with community, Consortium liaisons, and advisory board.
- Develop partnerships,
- Leverage resources,
- Education and Outreach plans

QUBES Consortium members

- **NIMBioS**
- **BioSIGMAA**
- **SMB**
- **MBI**
- **AAAS**
- **HHMI**
- **BioQUEST**
- **ESA**
- **TWS**
- **12 other institutions and organizations**



QUBES Activities

to connect the
community



BIO-
SIGMAA
and NSF
RCN
Incubator
Grant
start

Development team meeting at RC

Summit at NIMBioS at UT Knoxville

Submitted NSF IUSE
Ideas Lab Proposal

\$2.9 million, 5-year
NSF IUSE award

QUBESHub,
HubZero
site online

2nd Summit with
Data Inquiry RCN
at NESCent

Jan
2014

Mar

May

June

Sept

January
2015

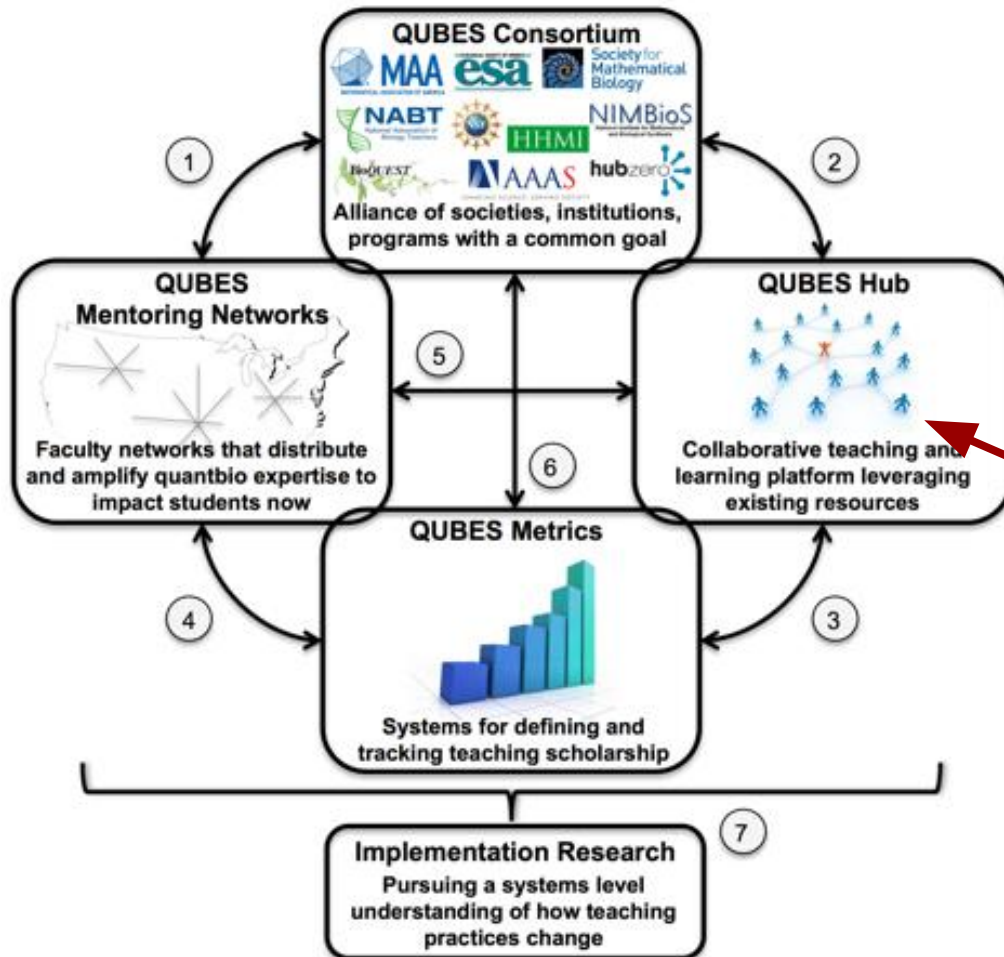
February

Consortium vision for QUBES

A word cloud visualization of the Consortium vision for QUBES. The words are arranged in a circular pattern, with the most prominent words in the center and smaller words towards the edges. The words are in various shades of blue and green. The central words are 'biology', 'community', 'faculty', 'mathematics', and 'quantitative'. Other prominent words include 'develop', 'support', 'share', 'build', and 'collaboration'. Smaller words include 'adopt around', 'broadly', 'career change', 'confidence', 'curriculum', 'defined', 'education', 'facilitate', 'implement', 'including', 'information', 'interface', 'letters', 'literacy', 'mentoring methods', 'motivate multiple', 'options organizations particular pedagogical populations professional promote', 'public', 'questions reach research rising', 'skills storm synergy training underserved', and 'understanding uses vision'.

biology
community
faculty
mathematics
quantitative
develop
support
share
build
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QUBES Hub



Virtual space to bring the math-biology education community together.

Hub Team
w/HubZero:

M. Drew LaMar

Bob Sheehy

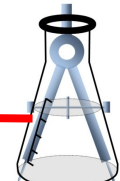
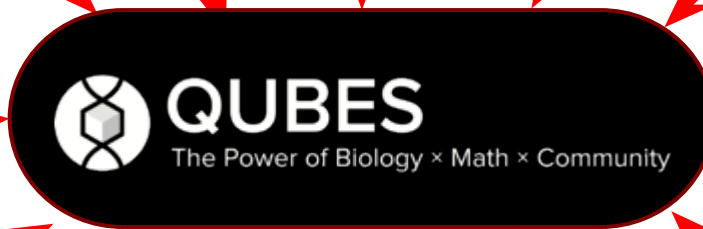
DB Poli

Jennifer Cartier

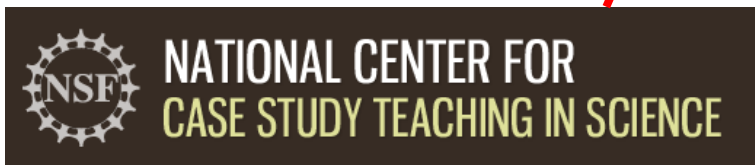
Michael McLennan

J. Patrick Mulligan

MERLOT II

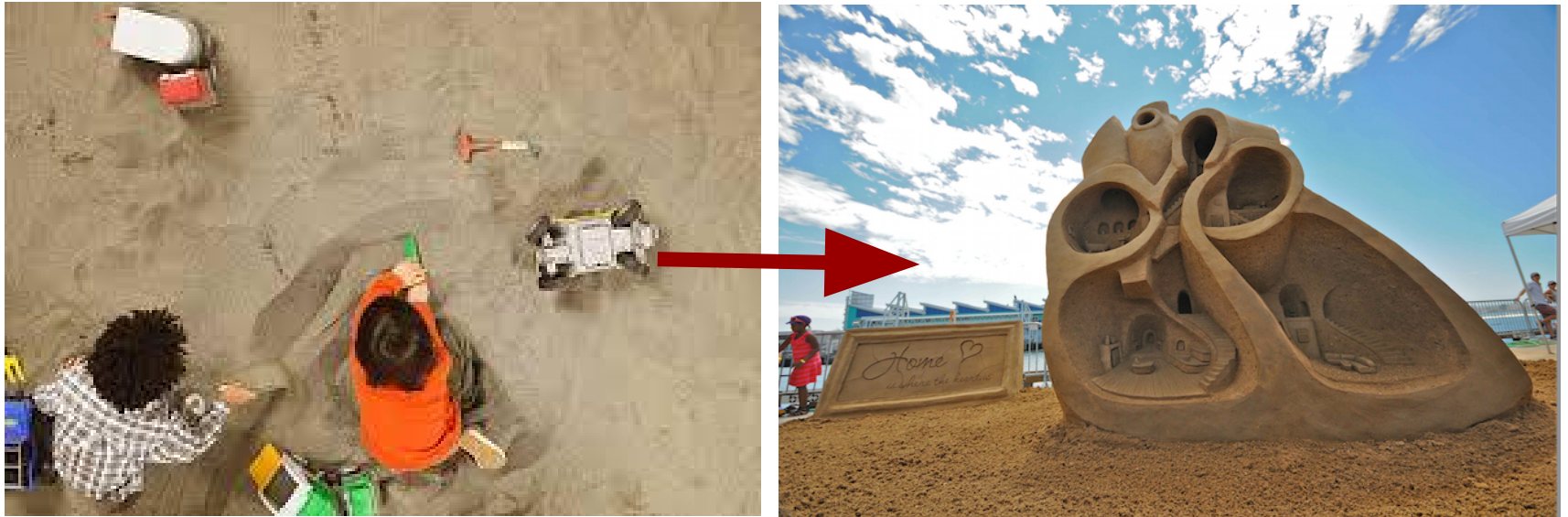


BMC-IMB



Personal Pages

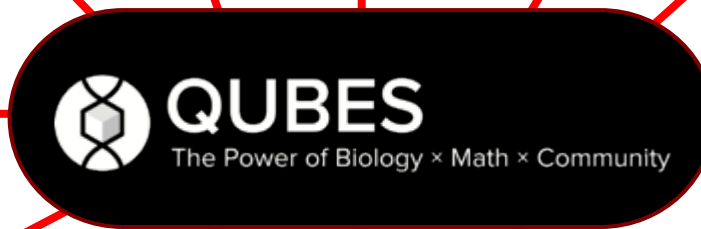
From Idea to Product



Collaboration space

<http://www.webmd.com/parenting/d2n-stopping-germs-12/slideshow-kids-germs-handwashing>
<http://sf.funcheap.com/event-series/carve-san-francisco-sandcastle-building-contest/>

MERLOT II



Personal Pages

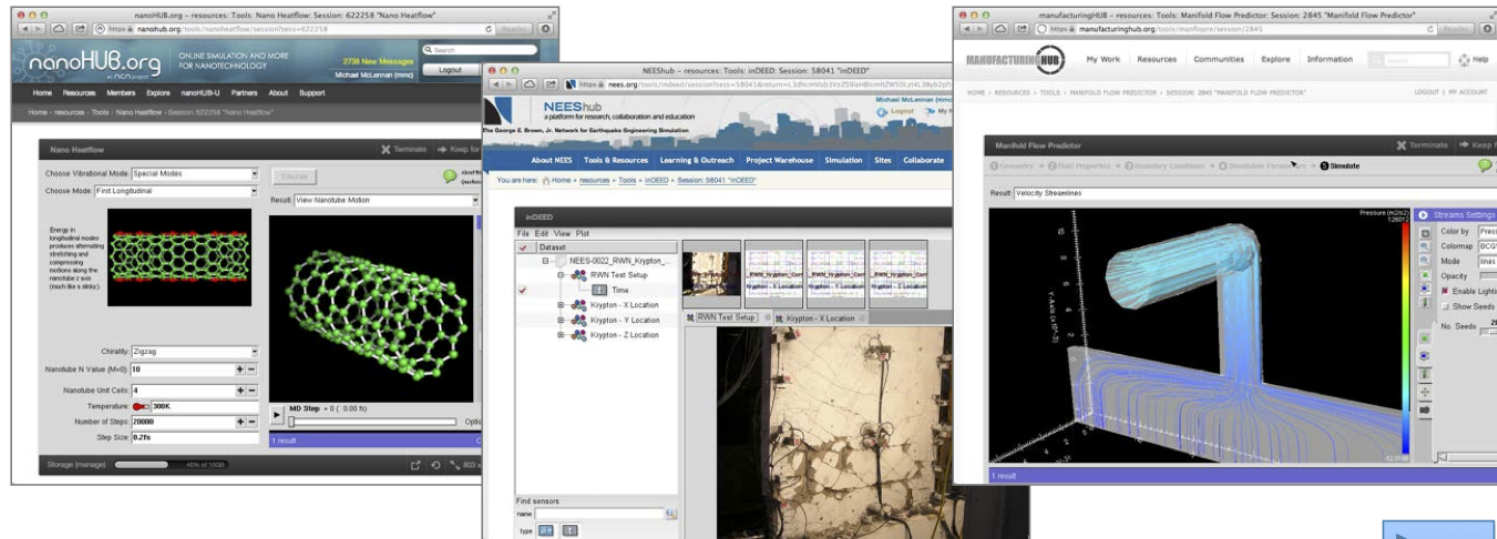
Vision for QUBES Hub

1. Foster collaboration beyond silos (language, place)

Vision for QUBES Hub

1. Foster collaboration beyond silos (language!)
2. A hub/repository for multiple types of curriculum/research objects, such as:
 - a. labs, data, modules, assessments (*version control, customizable*)
 - b. web-based simulators/data analyzers
 - c. implementation guides

HUBzero: Simulation/Modeling Tools



- ✓ Powerful research codes
- ✓ Uploaded by researchers in the community
- ✓ Run on cloud/grid/cluster resources
- ✓ Integrated visualization



Vision for QUBES Hub

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3. Nested tagging system, a powerful search engine, and fluid content navigation tools

Vision for QUBES Hub

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 - c. implementation guides
3. Nested tagging system, a powerful search engine, and fluid content navigation tools
4. Ability for informal and formal peer review

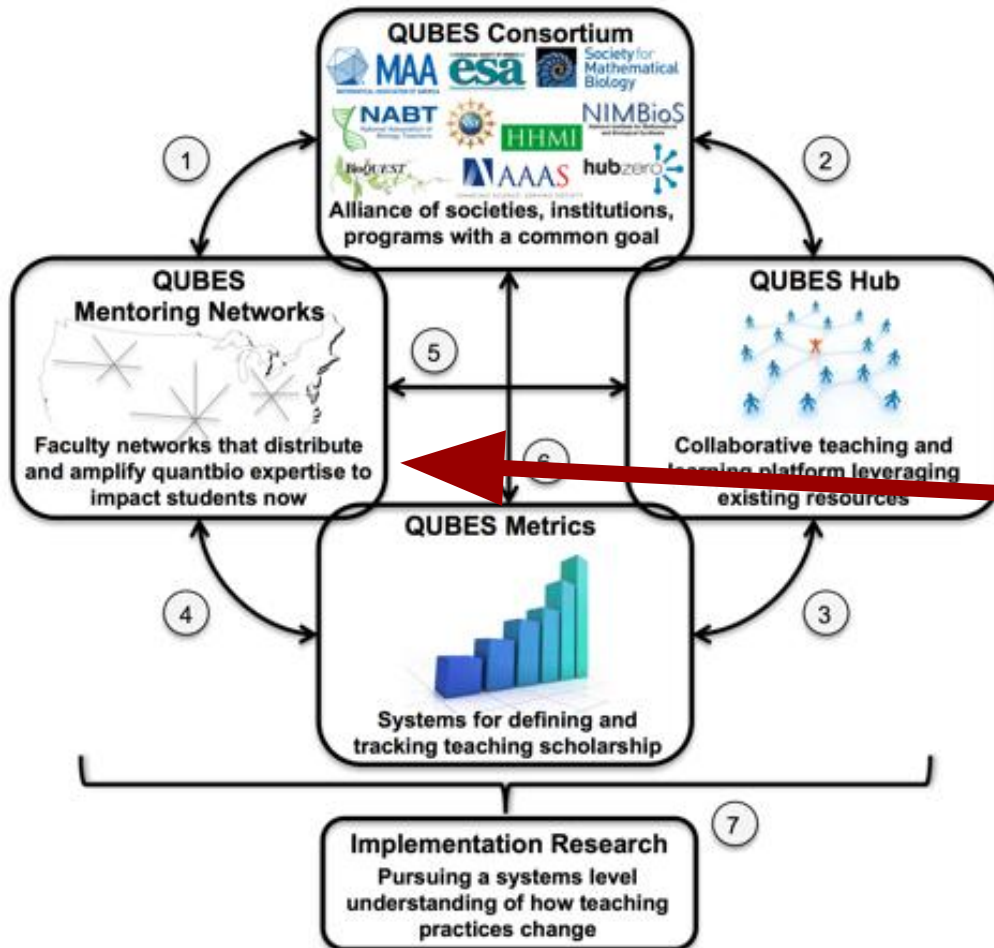
More than just a repository

With the ability to like, rate, dynamically add and link content.

A HUB where curriculum content can be *created*, **shared**, **modified**, **stored**, and **organized**, all in a heavily **social**, **adaptive** and **collaborative** context.



QUBES Mentoring Networks - Backbone of the QUBES community



- Distributing Faculty Expertise
- Mentoring programs
 - F2F and virtual
- Community curriculum development and assessment
- Senior Personnel
 - Sam Donovan
 - Jeremy Wodjak
 - Kristin Jenkins



QUBES

The Power of **Biology** × **Math** × **Community**

[HOME](#)[RESOURCES](#)[COMMUNITY](#)[ABOUT](#)[SUPPORT](#)[EXPLORE](#)

QUANTITATIVE UNDERGRADUATE BIOLOGY EDUCATION AND SYNTHESIS

The Power of Biology × Math × Community

[Learn more about QUBES...](#)



QUBES Consortium



MAA
MATHEMATICAL ASSOCIATION OF AMERICA

esa
ECOLOGICAL SOCIETY OF AMERICA



**Society for
Mathematical
Biology**



NABT
National Association of
Biology Teachers



HHMI

NIMBioS
National Institute for Mathematical
and Biological Synthesis



AAAS
ADVANCING SCIENCE, SERVING SOCIETY

hubzero

**Alliance of societies, institutions,
programs with a common goal**

FEATURED IN COMMUNITY

BioQUEST
CURRICULUM CONSORTIUM

hhmi

ScienceCaseNet

*Count the Ways:
Engaging Students in
Quantitative Biology
Education*

June 13-20, 2015
Harvey Mudd College

FEATURED IN RESOURCES



COPASI

Octave

R Studio

NetLogo

NEWS AND EVENTS

FEB 22, 2015

[NSF funding opportunity: BIGDATA program](#)

MAR 30, 2015

[SABER 2015 Abstract Deadline](#)

Thank you!!



NSF grants DBI-1346584
and DUE-1446258
BIO SIGMAA, NIMBioS

- Hannah Callender
- Bodine, Gross, and Lenhart, Princeton Press for draft book use
- Richard M. Schori (OSU, attitudes survey)

